

This book has permission to use the "N&K method of COLORS".

10) Question: In the function $f(x) = bx^2 + 15$, "b" is a constant. If " $f(3) = 33$ ", find the value of $f(5)$.

- A) 65 changed
- B) 70
- C) 75
- D) 80

For speed, while solving something similar, only THINK the words in blue; WRITE only the words in other COLORS.

Solution:

Given 1) $f(x) = bx^2 + 15$
 2) $f(3) = 33$
 Find $f(5) = ?$

Road Map of Solution:

First, Using the given statements, 1 & 2, find the value of "b".

Second, To find the value of $f(5)$; substitute the value of "b" and " $x = 5$ " in the given first statement.

Given

1st statement $f(x) = bx^2 + 15$ equation # 1
 2nd statement $f(3) = 33$ equation # 2

Solving eq # 1 for " $x = 3$ ", we get

$$\begin{aligned} f(x) &= bx^2 + 15 \\ f(x) &= b(\blacksquare)^2 + 15 \\ f(3) &= b(\blacksquare)^2 + 15 \\ f(3) &= b(9) + 15 \end{aligned}$$

Substituting $f(3) = 33$ in the equation above, we get,

$$\begin{aligned} 33 &= b(9) + 15 \\ -15 + \{ 33 \} &= \{ b(9) + 15 \} - 15 \\ -15 + 33 &= b(9) + 15 - 15 \\ 18 &= b(9) \quad \dots \quad \text{equation \# 3} \end{aligned}$$

Multiplying both sides of the equation # 3 with $\frac{1}{9}$

$$\begin{aligned} \left(\frac{1}{9}\right) \times \{18\} &= \{b(9)\} \times \left(\frac{1}{9}\right) \quad \dots \quad \text{equation \# 3b} \\ \left(\frac{1}{9}\right) \times \{18\} &= \{b(9)\} \times \left(\frac{1}{9}\right) \\ \left(\frac{1}{9}\right) \times \{ 2 \} &= \{b(1)\} \times \left(\frac{1}{9}\right) \\ (1) \times \{ 2 \} &= \{b(1)\} \times (1) \\ \{ 2 \} &= \{b\} \\ 2 &= b \quad \dots \quad \text{equation \# 3c} \end{aligned}$$

From eq#s 1 & 3c, we get,

$$\begin{aligned} f(x) &= bx^2 + 15 \\ f(x) &= (b)(x)^2 + 15 \\ f(5) &= (2)(5)^2 + 15 \\ f(5) &= (2)(25) + 15 \\ f(5) &= 50 + 15 \end{aligned}$$

$f(5) = 65$ Answer (A)
